

Exercise 34

For the following exercises, perform the indicated operation and express the result as a simplified complex number.

$$\frac{2 - 3i}{4 + 3i}$$

Solution

Start by making the denominator real. Then use the distributive property.

$$\begin{aligned}\frac{2 - 3i}{4 + 3i} \\ \frac{2 - 3i}{4 + 3i} \times \frac{4 - 3i}{4 - 3i} \\ \frac{(2 - 3i)(4 - 3i)}{(4 + 3i)(4 - 3i)} \\ \frac{8 - 6i - 12i + 9i^2}{16 - 12i + 12i - 9i^2} \\ \frac{8 - 18i + 9(-1)}{16 - 9(-1)} \\ \frac{8 - 18i - 9}{16 + 9} \\ \frac{-1 - 18i}{25} \\ \frac{1}{25}(-1 - 18i) \\ -\frac{1}{25} - \frac{18}{25}i\end{aligned}$$